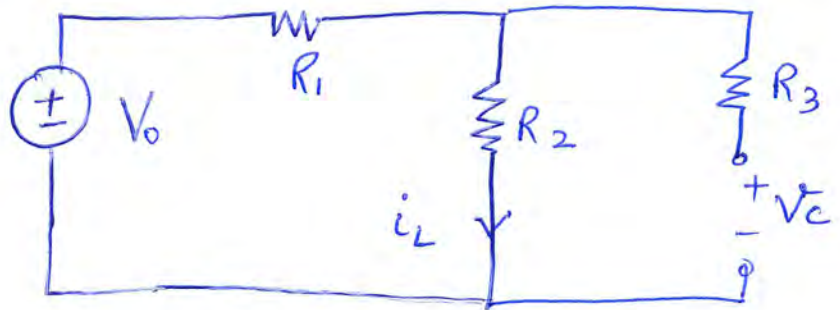


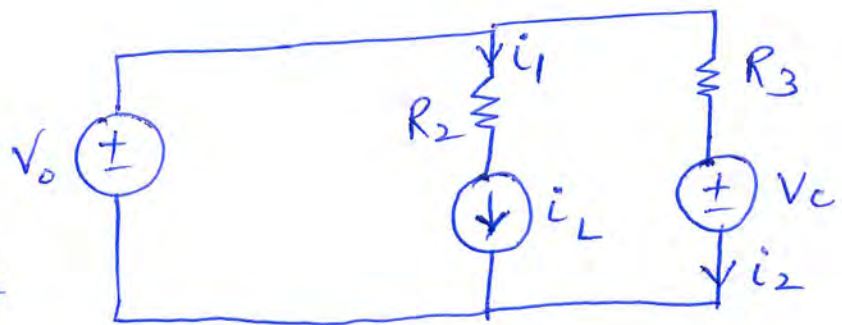
PROBLEM 015-20EVALUATION OF INITIAL CONDITIONSAt $t = 0^-$

$$i_L = \frac{V_0}{R_1 + R_2}$$

$$V_c = \frac{R_2}{R_1 + R_2} V_0$$

At $t = 0^+$

$$\Rightarrow i_1(0^+) = i_L \quad \text{A}$$



$$i_2(0^+) = \frac{V_0 - V_c}{R_3} = \frac{V_0 (R_1)}{R_3 (R_1 + R_2)} \quad \text{A}$$

Loop 1: (V_0 , R_2 and L)

Equation:
$$V_0 = i_1 R_2 + L \frac{di_1}{dt}$$

$$\Rightarrow L \frac{di_1}{dt} = V_0 - i_1 R_2$$

$$\Rightarrow \frac{di_1}{dt}(0^+) = \frac{V_0}{L} - \frac{V_0 R_2}{L(R_1 + R_2)} = \frac{V_0}{L} \frac{R_1}{(R_1 + R_2)} \quad \text{A/sec}$$

Loop 2: V_0 , R_3 and C

Equation:
$$V_0 = i_2 R_3 + \frac{1}{C} \int i_2 dt \Rightarrow 0 = R_3 \frac{di_2}{dt} + \frac{i_2}{C}$$

$$\Rightarrow \frac{di_2}{dt} = - \frac{i_2}{R_3 C}$$

$$\Rightarrow \frac{di_2}{dt} (0^+) = \frac{-V_0 R_1}{R_3^2 (R_1 + R_2)} \quad \text{A/sec.}$$

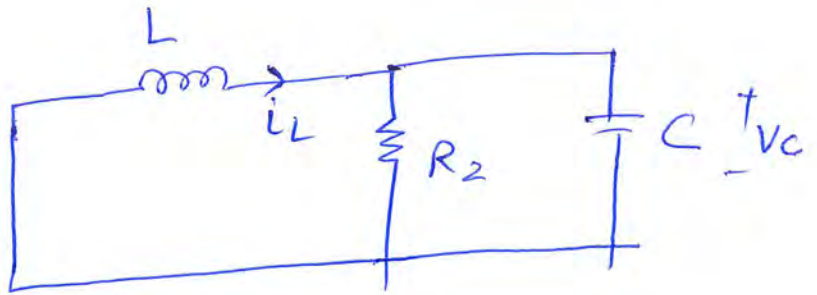
Problem 02

5-21

At $t = 0^-$

$$i_L = 0$$

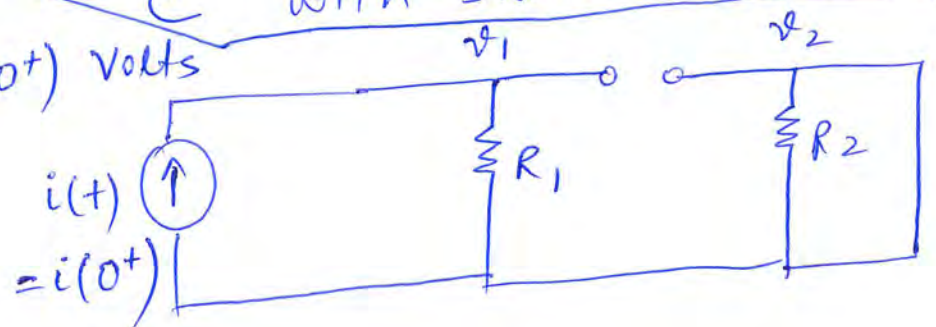
$$v_C = 0$$



At $t = 0^+$; Replace L with open circuit
 and C with short circuit

$$v_1 = R_1 i(t) = R_1 i(0^+) \text{ Volts}$$

$$v_2 = 0 \text{ Volts}$$



Node ① Equation

$$\frac{v_1}{R_1} + \frac{1}{L} \int (v_1 - v_2) dt = i(t)$$

$$\frac{1}{R_1} \frac{dv_1}{dt} + \frac{v_1 - v_2}{L} = \frac{di}{dt}$$

$$\Rightarrow \frac{dv_1}{dt} = R_1 \frac{di}{dt} + R_1 \frac{v_2 - v_1}{L}$$

$$\text{at } t=0^+ \quad \frac{dv_1}{dt} = R_1 \frac{di(0^+)}{dt} - R_1 \frac{i(0^+)}{L}$$

Node ② Equation

$$\frac{v_2}{R_2} + \frac{C dv_2}{dt} + \frac{1}{L} \int (v_2 - v_1) dt = 0$$

At $t = 0^+$ $i_L = 0$ at $t = 0^+$

V/sec

$$\Rightarrow \boxed{\frac{dv_2}{dt} = 0} \text{ at } t = 0^+$$

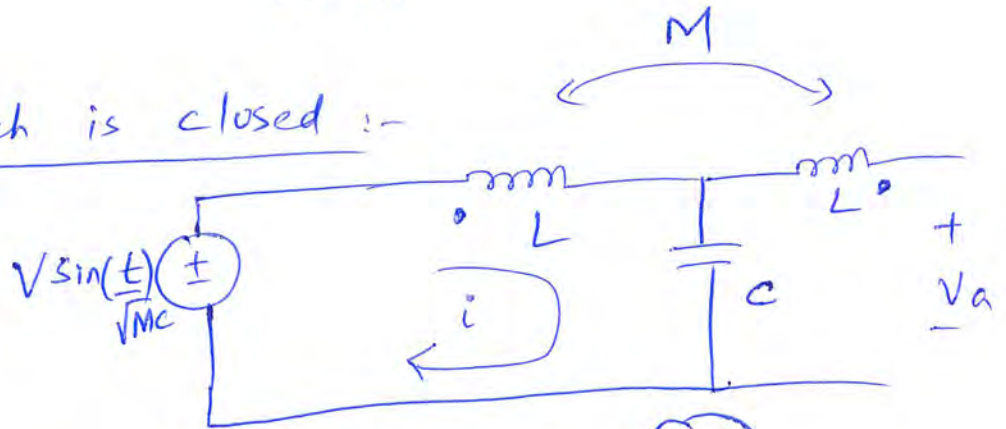
Problem 03

5-24

~~At~~ At $t=0^-$; * current through inductor is zero
 * voltage across capacitor is zero

After the switch is closed :-

$i(0^+) = 0$
Loop Equation



$$V \sin \frac{t}{\sqrt{MC}} + L \frac{di}{dt} + \underbrace{\frac{1}{C} \int i dt}_{0 \text{ at } t=0^+} = 0 \quad \text{--- (01)}$$

$$\Rightarrow \frac{di(0^+)}{dt} = - \frac{V}{L} \sin \left(\frac{t}{\sqrt{MC}} \right) \Big|_{t=0^+} = 0$$

$$\underline{V_a} :- \quad V_a = \frac{1}{C} \int i dt + M \frac{di}{dt} \quad \text{--- (02)}$$

$$\underline{t=0^+} \quad \boxed{V_a = 0}$$

Taking derivative of (01) $\Rightarrow \frac{d^2 i}{dt^2} (0^+) = \frac{V}{\sqrt{MC}}$

Taking (02) $\Rightarrow \frac{dV_a}{dt} (0^+) = \frac{V}{L} \sqrt{\frac{M}{C}}$

Taking twice

$$\frac{d^2 V_a}{dt^2} = \frac{1}{C} \frac{di}{dt} + M \frac{d^3 i}{dt^3} \Rightarrow \underbrace{\frac{di}{dt}}_{0 \text{ at } t=0^+} \Rightarrow \boxed{\frac{d^2 V_a}{dt^2} (0^+) = 0}$$