EE 240 Circuits I

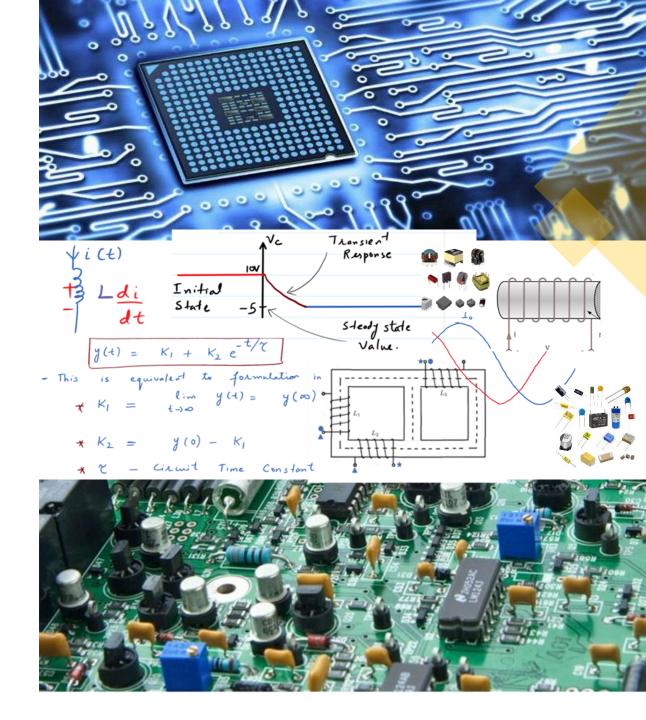
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https://www.zubairkhalid.org/ee240_2020.html

Topics:

- R,L,C summary
- Series, parallel connection



Resistor, Capacitor, Inductor (R,C,L)

Summary:

R,C and L are passive elements

Resistor, R



$$v = iR$$

 $i = \frac{v}{R}$

Capacitor, C



$$v(t) = \frac{1}{C} \int_{\tau = -\infty}^{t} i(\tau) d\tau \qquad i = C \frac{dv}{dt} \qquad w = \frac{1}{2} C v^2$$

Inductor, ${\cal L}$



$$v = L \frac{di}{dt}$$

$$\Psi(t) = \frac{1}{L} \int_{\tau = -\infty^t} v(\tau) d\tau \qquad w = \frac{1}{2} L i^2 \qquad \Psi = L i$$

i(t)

$$\mathbf{x} \neq v(t) \quad \mathbf{C} = v(t) \quad \mathbf{L} \neq v(t)$$

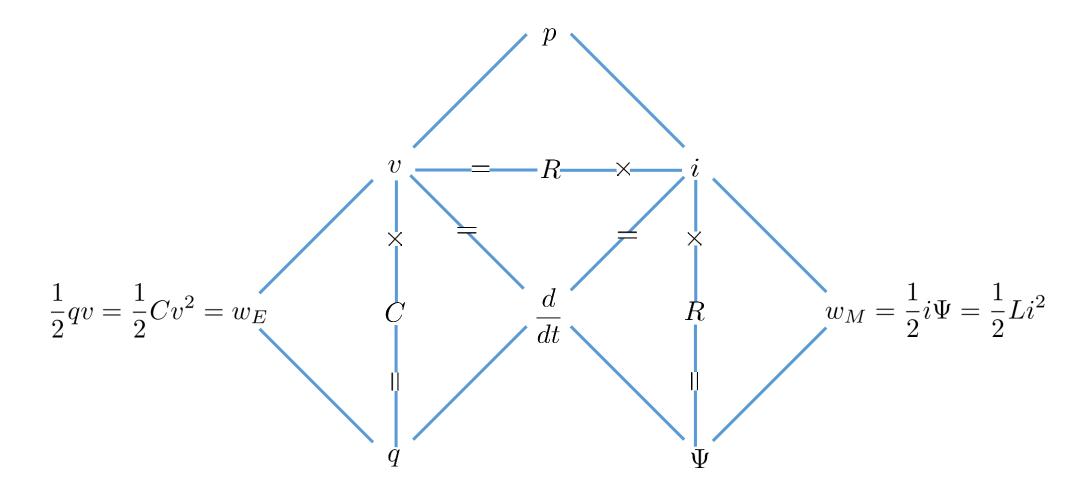
i(t)

i(t)

$$w(t) = \int_{\tau = -\infty}^{t} p(\tau) d\tau \qquad p = vi = i^2 R = \frac{v^2}{R}$$

Resistor, Capacitor, Inductor (R,C,L)

Encapsulated:

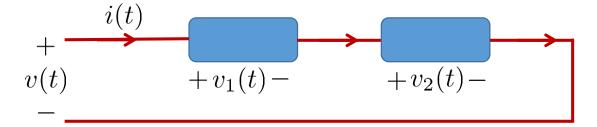




Elements and Sources in Series/Parallel

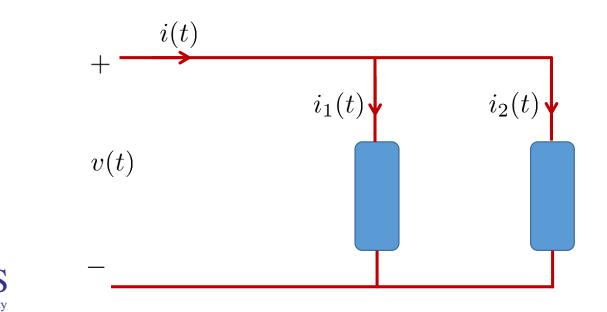
Series Connection:

Idea: same current, voltage is divided



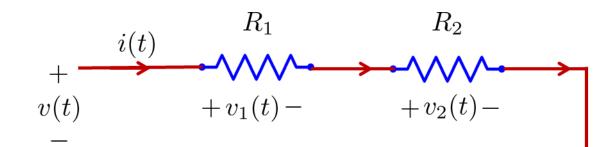
Parallel Connection:

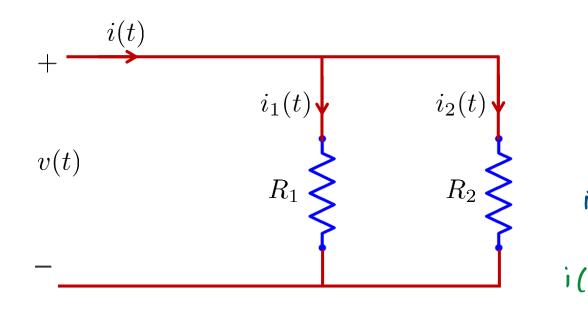
Idea: same voltage, current is divided





Resistors in Series or Parallel





$$i_{1}(t) = \frac{v(t)}{R_{1}}, \quad i_{2} = \frac{v(t)}{R_{2}}$$

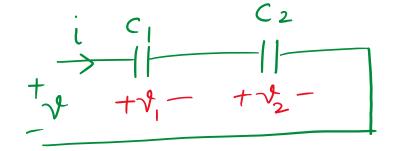
$$(t) = i_{1} + i_{2} = v(t) \left(\frac{1}{R_{1}} + \frac{1}{R_{2}}\right)$$

$$t) = \frac{v(t)}{R_{eq}} \implies \prod_{Req} = \frac{1}{R_{1}} + \frac{1}{R_{2}}$$

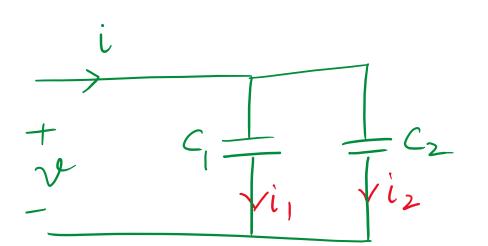
$$Req = \frac{R_{1}R_{2}}{R_{1} + R_{2}}$$



Capacitors in Series or Parallel



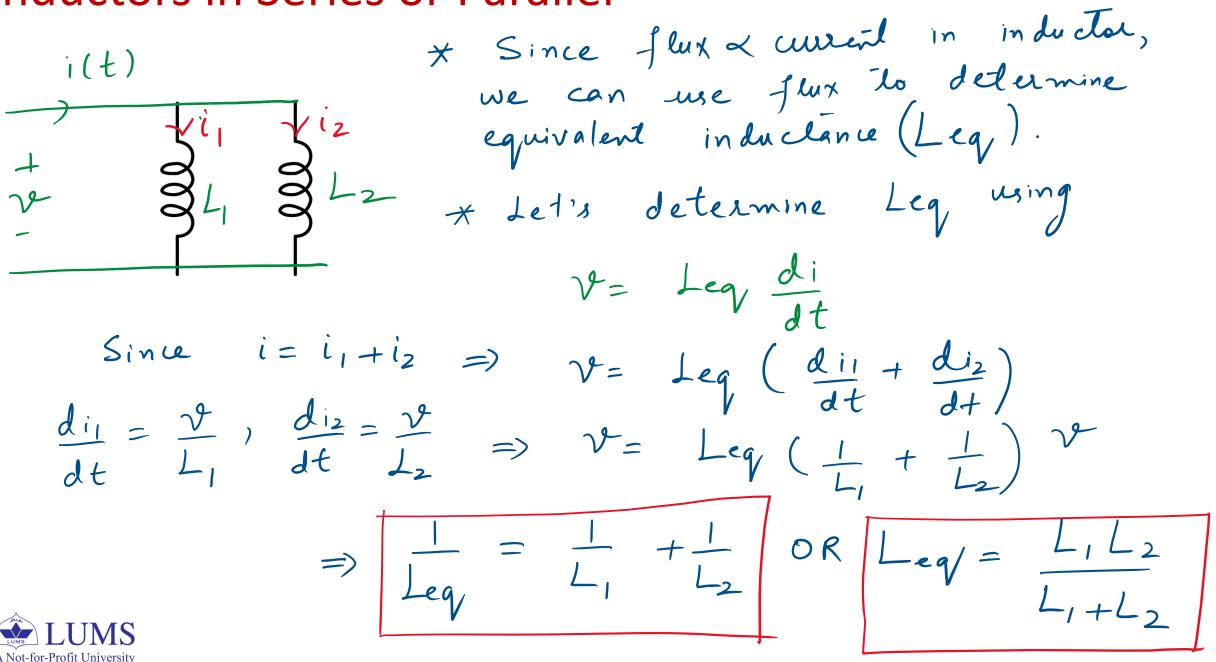
Same current \leftarrow same charge \Rightarrow i $\leftrightarrow q$ $\mathcal{V}_{1} = \frac{q}{C_{1}}, \quad \mathcal{V}_{2} = \frac{q}{C_{2}} \Rightarrow \mathcal{V} = Q\left(\frac{1}{C_{1}} + \frac{1}{C_{2}}\right)$ $L = \frac{q_{\perp}}{Q_{\perp}} \Rightarrow \frac{1}{C_{eq}} = \frac{1}{C_{\perp}} + \frac{1}{C_{2}} \Rightarrow C_{eq} = \frac{C_{1}C_{2}}{C_{1}+C_{2}}$ $C_{eq} = \frac{C_{1}C_{2}}{C_{1}+C_{2}}$



Similarly $C_{1} + C_{2}$ Ceq =



Inductors in Series or Parallel

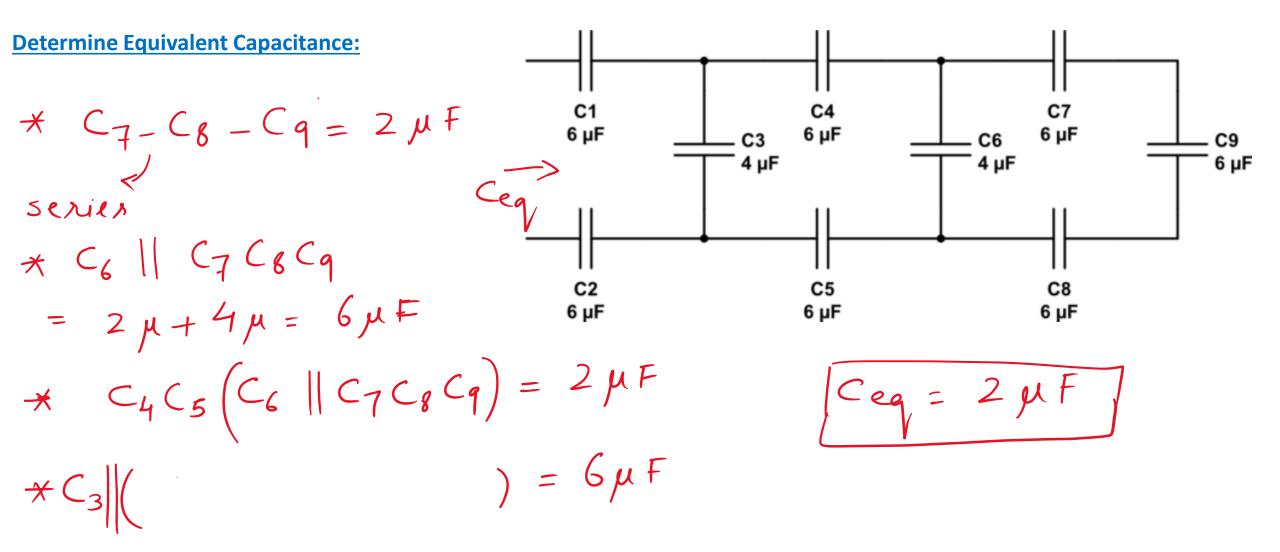


Inductors in Series or Parallel

 $\gamma = \gamma + \gamma_2$ 1-2 $+ \sqrt{1}$ $(L_1 + L_2) \frac{di}{dt}$ =) \mathcal{V} = + 42 ·cg/ = =)



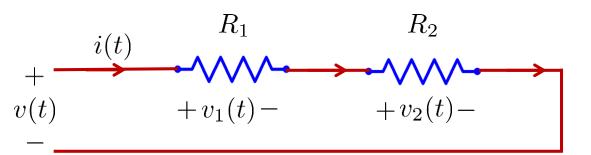
Example: Equivalent Capacitance

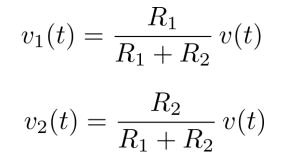


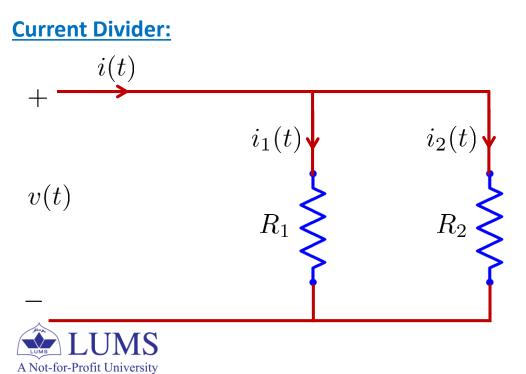


Example: Voltage and Current Divider Rules

Voltage Divider:







$$i_1(t) = \frac{R_2}{R_1 + R_2} i(t)$$
$$i_2(t) = \frac{R_1}{R_1 + R_2} i(t)$$