## LAHORE UNIVERSITY OF MANAGEMENT SCIENCES Department of Electrical Engineering

EE240 Circuits I Quiz 04 Solutions

Name:
Campus ID:
Fotal Marks: 10
Fime Duration: 20 minutes

## **Question 1** (10 marks)

In a first-order circuit given below, the switch is operated from position a to position b at t = 0.



(a) [1 mark] Determine the voltage across capacitor at  $t = 0^-$ . Solution:

$$v_c(0^-) = 30\frac{3}{9} = 10\,V$$

(b) [2 marks] Determine i(t) at  $t = 0^+$ .

**Solution:** For  $t \ge 0$ ,  $v_c(t)$  and i(t) are related by  $v_c(t) = \frac{1}{2} \int i dt$ . Applying KCL yields

$$\frac{v_c}{3} + \frac{v_c - 12}{6} + i = 0 \quad \Rightarrow \quad \frac{v_c}{2} - 2 + i = 0.$$

We can evaluate this this at t = 0 to obtain  $i(0^+) = 2 - 5 = -3 A$ .

(c) [2 marks] Write down the differential equation, in terms of i(t), describing the circuit after the switch is operated, that is, for  $t \ge 0$ .

Solution: Using the equation formulated in part(b), we obtain

$$\frac{1}{4}\int i dt + i = 2, \quad \Rightarrow \quad \frac{di}{dt} + \frac{i}{4} = 0$$

(d) [1 mark] Determine i(t) at  $t = \infty$ . Solution:

$$i(0^+) = 0A$$

(e) [3 marks] Determine i(t) for all values of t and plot (and label) it.

**Solution:** i(t) = 0 for t < 0. Using differential equation formulation, we determine

$$i(t) = Ke^{-t/4}$$

where K = -3 using the initial conditions.

Alternatively, we can start with the following solution:

$$i(t) = K_1 + K_2 e^{-t/\tau}.$$

We can find  $K_1 = 0$  and  $K_2 = -3$  using initial and final conditions and  $\tau = R_{eq}C = 4s$ , where  $R_{eq} = 6||3 = 2\Omega$ .

(f) [1 mark] On the plot that is obtained in part (e), superimpose plot of i(t) for if 2 F capacitor is replaced with 1 F capacitor.

**Solution:** For C = 1F, time constant is halved and therefore the current decays to zero relatively faster.