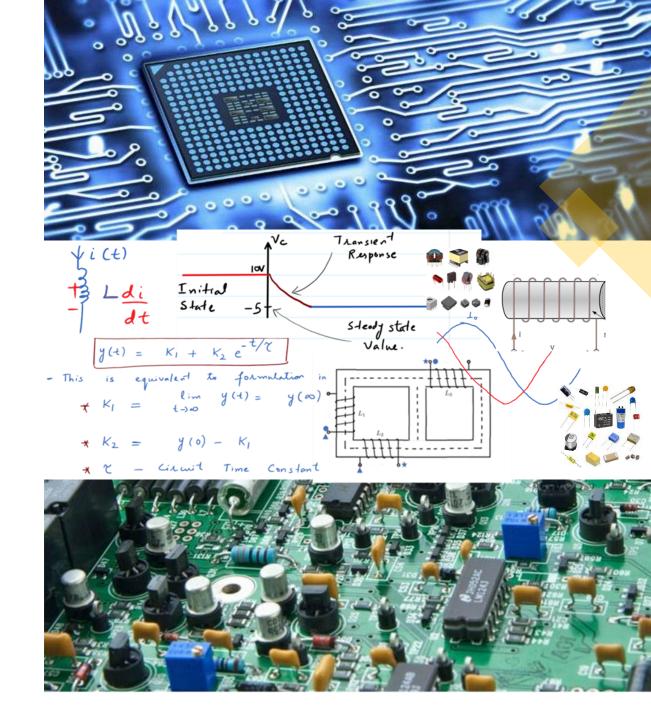
EE 240 Circuits I

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https://www.zubairkhalid.org/ee240_2021.html

- Duality



Duality in Circuits

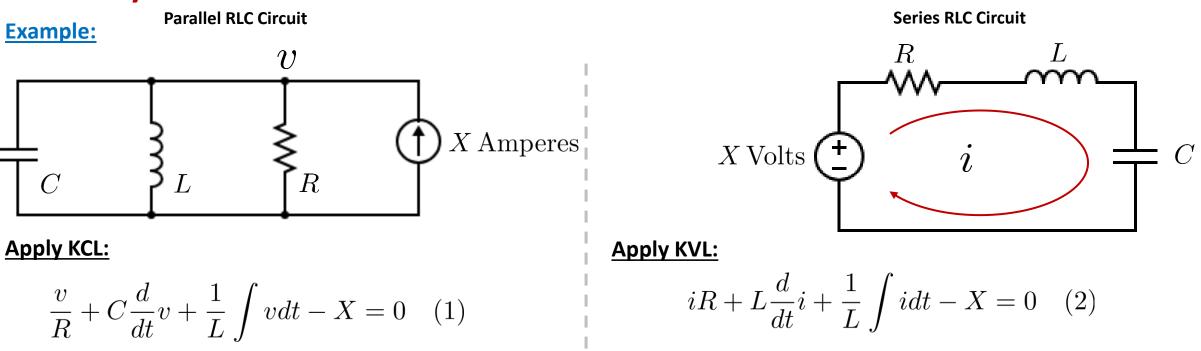
Overview

The concept is that the voltage or current in a circuit behaves in analogous manner as the current or voltage in a dual circuit.

- Ohm's law is a simple example, that is, we have v = iR. This is equivalent to i=v(1/R). If we current and voltage are swapped in the first equation and R is replaced with (1/R), we obtain a second equation. We refer to this as 1) voltage and current are dual of each other and 2) (1/R) is a dual of (R).
- Similarly KCL and KVL are analogous.
- This similarity is part of large pattern of identical behaviour patterns between voltage and current in the network.
- Let's analyse series RLC and parallel RLC networks.



Duality in Circuits

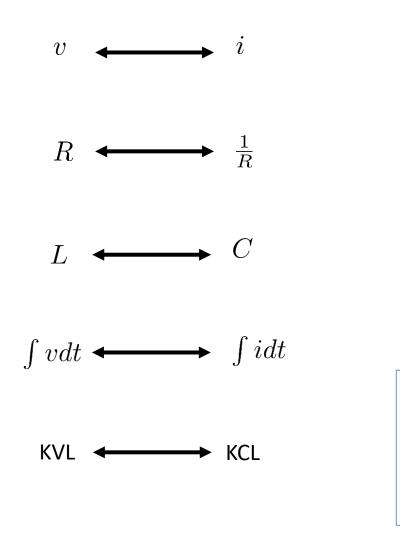


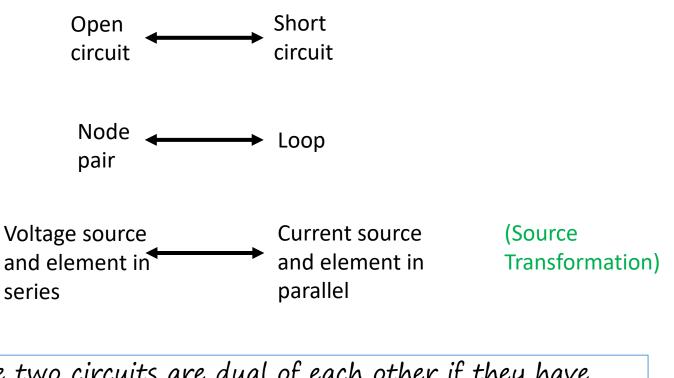
- Note the similarity between the resulting integro-differential equation.
- If we know the solution of one circuit, it can be utilized to readily obtain the solution of the other circuit.
- The solution of (1) yields v(t) in terms of R,L,C and X.
- The solution of (2) yields i(t) in terms of R,L,C and X.
- If we replace v(t) with i(t), C with L, L with C, R with (1/R) in equation (1), we obtain equation (2).
- Noting this, we can make these subsititutions in the solution v(t) to determine the solution i(t).



Duality in Circuits

Dual Quantities or Elements:





 The two circuits are dual of each other if they have the same network equations with dual quantities replaced. For a given circuit, we can determine the dual circuit. Let's learn the graphical construction of the dual circuit.



Graphical Construction of a Dual Circuit

<u>Step 01:</u>

- In a given circuit, place a node inside each loop and place and add an add one additional node (a datum node) outside the circuit.
- On a separate space, arrange the same numbered node on a separate sheet.

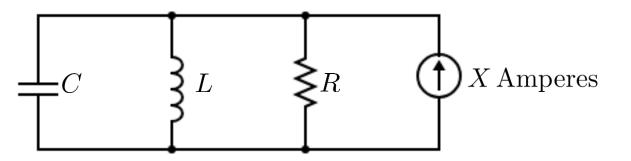
<u>Step 02:</u>

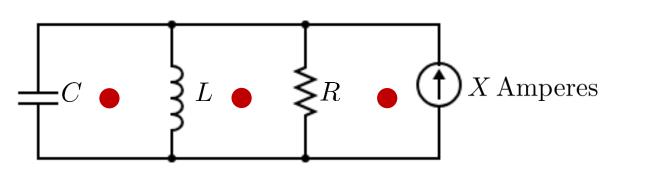
- Draw lines from node to node through elements in the original network only traversing one element at one time.
- For each element traversed from one node to the other in the original network, connect the dual element form the list between a pair of nodes in the dual network.
- Continue this process until the number of possible paths through single element is exhausted.

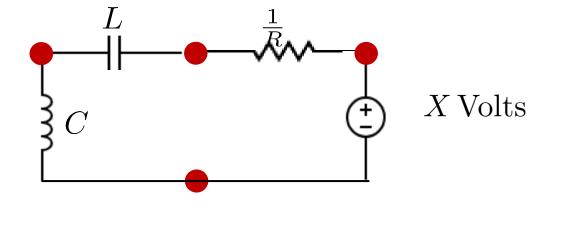


Graphical Construction of a Dual Circuit

Example:





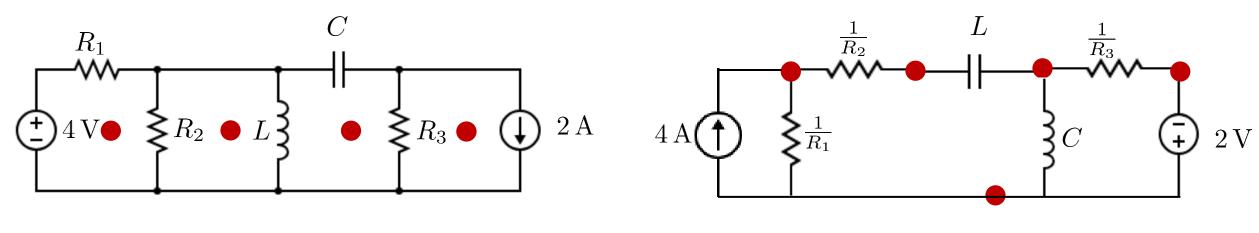


Dual Circuit



Graphical Construction of a Dual Circuit

Example:



Dual Circuit

